# Math 141 Challenge Exam Information <br> Mathematics Department San Diego Miramar College 

## Do not attempt the Math 141 Challenge Exam unless you are confident that you can successfully answer questions regarding the following topics.

- Define and distinguish between higher order polynomial functions and non-polynomial functions and relations, and analyze the graphs of functions by determining their domains and ranges.
- Analyze properties of functions and their graphs, including symmetries, increasing and decreasing intervals and their end behavior asymptotes.
- Prove algebraically and justify graphically when a function is one-to-one.
- Graph a variety of algebraic, rational, exponential, logarithmic, and trigonometric functions, and where applicable, use rigid and non-rigid transformations, intercepts and asymptotes.
- Perform algebraic operations on various functions including composition of functions, and determine the domain of the resulting function.
- Calculate the inverse of a one-to-one function, determine the domain and range of the inverse and describe the relation between their graphs.
- Solve equations and application problems involving exponential and logarithmic functions.
- Simplify difference quotients involving a variety of functions including polynomial, rational, trigonometric, exponential, and logarithmic functions.
- Apply a variety of root finding theorems and tests in order to factor polynomials or solve polynomial equations whose degree is higher than quadratic.
- Simplify rational expressions and expressions involving radicals that arise from calculus operations, such as those from the product or quotient rules.
- Determine the partial fraction decomposition of rational functions.
- Define, evaluate, describe and graph all trigonometric and inverse trigonometric functions, and solve equations involving these functions.
- Derive and prove fundamental trigonometric identities including the sum, difference, double and half angle identities.
- Apply the laws of sines and cosines in solving oblique triangles and in application problems.
- Represent complex numbers in standard, trigonometric and exponential forms and perform arithmetic operations with each.
- Perform algebraic operations involving matrices.
- Apply matrices in solving linear systems of equations.
- Compute the determinant of a square matrix, and apply determinants to various applications.
- Apply vector algebra to problems involving vector quantities.
- Perform the vector operations of the dot product and the cross product, and formulate their geometric interpretations.
- Analyze, identify, and graph the four conic sections.
- Solve systems of non-linear equations and inequalities, including those involving conic sections.
- Define and analyze sequences and series, including arithmetic and geometric sequences and series, find the sum of finite and infinite geometric series.
- Apply the binomial theorem to expand powers of binomial expressions.
- Prove elementary mathematical statements using the principle of Mathematical Induction.

